

GINA CODY SCHOOL OF ENGINEERING AND COMPUTER SCIENCE

ENGR 213

Applied Ordinary Differential Equations

Winter 2025

Course Instructor:

E-mail:

Office Hours: Lecture Hours:

Course Coordinator: Alexandre Paradis, <u>alexandre.paradis@concordia.ca</u>

Tutorials: Please see your class schedule for details

Tutorial Tutorial

Labs: N/A

Course Calendar Description:

This course introduces Engineering students to the theory and application of ordinary differential equations. Definition and terminology, initial-value problems, separable differential equations, linear equations, exact equations, solutions by substitution, linear models, orthogonal trajectories, complex numbers, form of complex numbers: powers and roots, theory: linear equations, homogeneous linear equations with constant coefficients, undetermined coefficients, variation of parameters, Cauchy-Euler equation, reduction of order, linear models: initial value, review of power series, power series solutions, theory, homogeneous linear systems, solution by diagonalization, non-homogeneous linear systems. Eigenvalues and eigenvectors.

Prerequisites: MATH 204 (cégep Mathematics 105) previously or concurrently; MATH 205 (cégep Mathematics 203).

Co-requisites: N/A

Specific Knowledge and Skills Needed for this Course:

Students taking this course are expected to have sufficient knowledge of the following topics. Should you have difficulties in any of these topics, you are strongly encouraged to review them before the DNE deadline.

- Fundamental Algebraic Manipulation
- o Calculus of a Single Variable (Differentials and Integrals)
- o Basic Matrix and Vector knowledge

Course materials

- **Required Textbook**: <u>Required textbook(s)</u>: Advanced Engineering Mathematics, by Dennis G. Zill and Warren S. Wright, 7th Edition¹, Published by Jones and Bartlett.
- **Instructor's lecture notes:** will be posted in Moodle course management site

¹ Please note that 5th and 6th editions have very minimal difference with the 7th section. Some exercises at the end of each section might have been re-ordered.

Grading

| Assessment Tool | Weight |
|---|--------|
| Midterms during tutorials (2- 10% each) | 20% |
| Final | 60% |
| Project* | 5% |
| Quizzes* | 10% |
| WebWork* | 10% |
| Total | 100% |

*The grading scheme implies 5% bonus. However, the maximum combined mark for the three components (WebWork + Quizzes + Project) is 20%.

Passing Criteria:

- In order to pass the class, both your cumulative score and the final examination must be above 50%
- In the event of extraordinary circumstances beyond the University's control, the content and/or evaluation scheme in this course is subject to change.

WeBWorK: Every student will be given access to an online system called WeBWorK. Students are expected to submit assignments online using WeBWorK. Late assignments will not be accepted. Assignments contribute 10% to your final grade. Working regularly on the assignments is essential for success in this course. Students are also strongly encouraged to do as many problems as their time permits from the chapters of the textbooks listed below in this outline.

- The WeBWorK administrator is Nehleh Jafari; email: webwork.engr@concordia.ca, any questions related to WeBWorK assignments should be directed to him.
- Students are also responsible for topics covered in assignments that have not been presented in either the regular lectures or during tutorials.

General rules:

- If the student misses one mid-term test for a valid reason, acceptable by the course instructor, including illness, then the final examination will count for 70% of the total grade. If a student misses both midterms, the final exam will still be 70%.
- There will be <u>no replacements of quizzes</u> for any reason, including illness.
- Students are responsible for finding out the date of the final exam. The Examination Office posts the time and place of the final exam once the schedule becomes available. Any conflicts or problems with the scheduling of the final exam must be reported directly to the Examination Office. Students are expected to be available until the end of the final examination period. Conflicts due to travel plans will not be accommodated.

NOTE: Electronic communication devices (including cellphones and smartwatches) **will not be allowed** during examinations and are prohibited in the examination rooms. Only "Faculty Approved Calculators" will be allowed for midterm and final exams [SHARP EL-531 or CASIO FX-300MS]. See Moodle site for an extensive list of the calculators.

Tentative Course Schedule; suggested problems are from the 7ed of the book

| Topics | Week |
|---|------|
| Review of the following topics: | 1 |
| 1.1 Definition and Terminology; problems: 1,3,5,10,11,13,14,23, 33, 35, 37 | |
| 1.2 Initial Value Problems; problems: 7,9,11, 35, 38 | |
| 2.1 Solution curves without a solution; problems: 3, 4, 26, 27 | |
| 2.2 Separable Equations; problems: 7,9,13,19,25,27, 31 | 2 |
| 2.3 Linear Equations; problems: 7,9,23,27,31 | |
| 2.4 Exact Equations, integrating factors; problems: 3,5,9,15, 21, 27,29, 33, 35, 39 | |
| 2.5 Solutions by Substitution (Bernoulli, homogeneous, linear substitution); problems: | 3 |
| 5,7,9,13,17,19,21,25,27 | |
| 1.3 Differential Equations as Mathematical Models; problems: 1,5, 7, 9,10, 13,16,19 | |
| 2.7 Linear models (growth/decay, heating/cooling, circuits, mixtures); problems: | |
| 3,5,9,15,17,23,25,29,31, 37, 44 | |
| 2.8 Non-linear models (Population dynamics, logistic equation, leaking tank); problems: | 4 |
| 2,3,11,13,15,17, 19 | |

| 17.1 Complex numbers; problems: 1,3,7,11,15,25,27,29, 35,39 | | |
|---|----|--|
| 17.2 Powers and Roots; problems: 3,7,9,15,21,29, 30, 33 | 5 | |
| 3.1 Theory of Linear Equations; problems: 1,9,17, 19, 27 | | |
| 3.3 Homogeneous Linear Equations with Constant Coefficients problems: 3,5,9,13,15,17,21, 31, 35 | 6 | |
| 3.4 Undetermined Coefficients; problems: 1,3,7,11,15,19,23,31 | | |
| 3.5 Variation of Parameters; problems: 1,3, 7, 13,15,23 | | |
| 3.6 Cauchy Euler Equations; problems: 5,7,11, 19, 23,45 | | |
| 3.7 Nonlinear Equations, Reduction of Order; problems: 3,7,9, 11 | | |
| 3.8 Linear Models. Initial Value Problems (mass-spring systems, free motion) problems: 1, | | |
| 6,7,12,26, 27 | | |
| 3.8 Linear Models. Initial Value Problems (driven motion and LRC-circuits) problems: | | |
| 31,33, 37,45*,47*, 51 | | |
| 5.1 Power Series Solutions; problems: 1, 11, 19, 21, 25, 31 | | |
| 10.1 Theory of Linear Systems; problems: 1,3,7,18 | 10 | |
| 10.2 Homogeneous Linear Systems; problems: 1,3,7,9,21,31,35,37,48 | 11 | |
| 10.4 Non-Homogeneous Linear Systems; problems: 1,3,5, 9,17, 19, 30 | 12 | |
| | | |

^{*}more advance problems

Lab Details

N/A - no labs

Engineering Tools

N/A – no specific use of engineering tools

Details on Assessment Tools:

N/A

Other relevant information

N/A

Graduate Attributes:

The following is the list of graduate attributes (skills) that students use, learn and/or apply throughout the term.

| Graduate Attribute | Indicators | Level of Coverage | Assessment Results Reported |
|--------------------------------|---|----------------------|-----------------------------------|
| Knowledge base for engineering | Knowledge base of mathematics | Introductory | Yes |
| Problem Analysis | Problem Identification and Formulation Modeling Problem Solving | Introductory | Yes |
| Team Work | Ability to work in a team | Introductory | Yes |

Course Learning Outcomes (CLOs):
By the end of this semester, students are expected to master the following concepts.

| Course Learning Outcome | Related Graduate Attributes |
|-------------------------|-----------------------------|
|-------------------------|-----------------------------|

| Apply calculus to engineering problems. Extract all the pertinent information <i>vis-à-vis</i> the physics and practicality of the problem. This component is examined through applied problems in the final exam. | Knowledge base of mathematics PA/Problem Identification and Formulation PA/Modeling PA/Problem Solving |
|--|---|
| Learn how to work within a team. This is done through one or two Team Projects. | Knowledge base of mathematics PA/Problem Identification and Formulation PA/Modeling Analysis Team-Work |
| Develop the ability to work as part of a team: this is done through the participation in a team project and through some interactive tutorials | Team-Work |

Health and Safety Guidelines

All health and safety rules specific to this course can be found in the lab manual. General health and safety instructions and available health and safety trainings are discussed at:

Safety Programs - Concordia University

ON CAMPUS RESOURCES

Student may find the full list of available resources at:

- Important Services & Resources Concordia University
- A-Z Student Services Concordia University

While they are included in above mentioned two links, following list includes frequently searched services and resources available for students.

- 1. Academic Resources Concordia University
 - a. Academic integrity Concordia University
 - b. Undergraduate Calendar Concordia University
 - c. Graduate Calendar Concordia University (For Graduate Classes)
 - d. Academic dates Undergraduate Concordia University
 - e. <u>Important dates Graduate Concordia University</u> (For Graduate Classes)
 - f. Learning services Concordia University
 - g. Advocacy Concordia University
- 2. Health & Wellness Concordia University
 - a. Access Centre for Students with Disabilities Concordia University
 - b. Mental health Concordia University
- 3. Safety & security Concordia University
 - a. Security services Concordia University
 - b. Environmental Health and Safety Concordia University
 - c. Safety Training Concordia University
- 4. International students Concordia University